

# Aerovox®

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## Mitigation of Harmonics On Low-Voltage Power Systems

Presented by:  
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## What are Harmonics?

The term "harmonics" is used today to describe many power system problems. The following details some key concepts in understanding harmonic phenomena.

Any periodic wave can be described as a sum of sine waves with varying magnitude and frequency. This is known as a Fourier Series. Each term in the series is referred to as a harmonic of the fundamental frequency. In power systems, the fundamental frequency is 60 Hz and the harmonics are integer multiples of 60 Hz (180, 300, 420, etc.) Further, these waves are symmetrical about the vertical axis. One wave form that appears repeatedly in the analysis of harmonics is the square wave. Many harmonic producing loads generate voltage or current wave forms that can be closely matched with a square wave. These devices range from rectifiers to arc furnaces. The figure below illustrates a square wave in both the time and frequency domain.

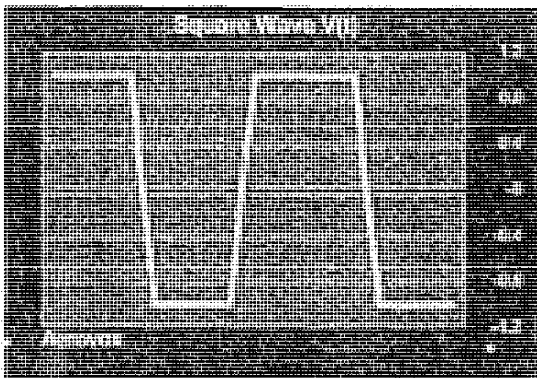


Figure 1

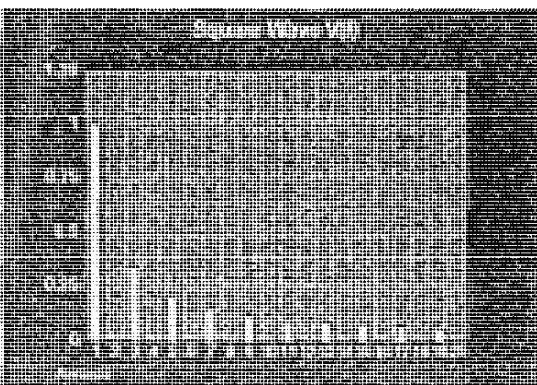


Figure 2

It should be noted that the term "harmonics" and "transients" are often used interchangeably; however, these two terms describe two very distinct phenomena. Harmonics are steady state occurrences while transients are, as the name implies, random. The following figure illustrates the difference between the two wave forms.

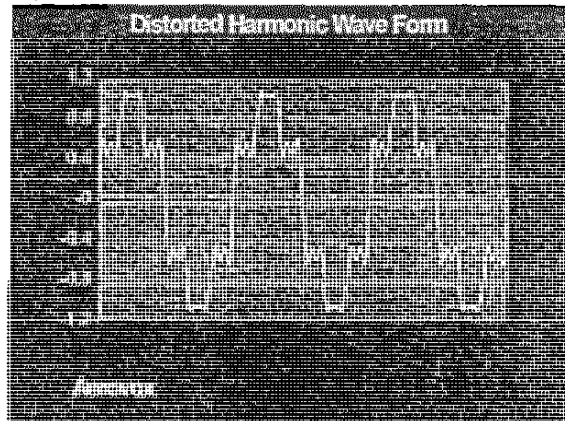


Figure 3

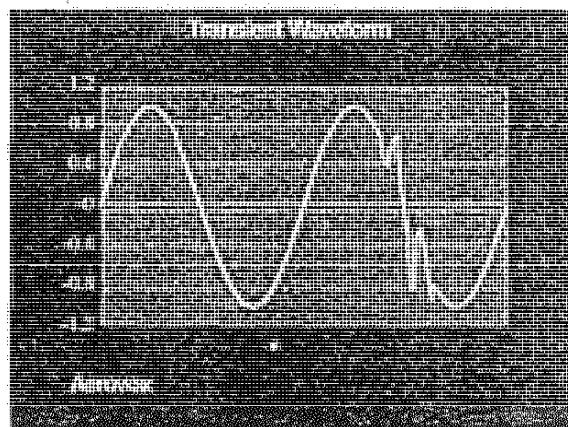


Figure 4

Total Harmonic Distortion (THD) is the quantity that is used to give a general definition of the "quality" of the current and voltage. The greater the value of THD, the more distorted the sine wave. THD is defined as follows:

$$THD = \frac{(V_2^2 + V_3^2 + \dots + V_n^2)^{1/2}}{V_1}$$

Where,  $V_2, V_3, \dots, V_n$  = Individual RMS harmonic Voltage Components and  $V_1$  = Fundamental frequency (60 Hz) RMS Voltage.

# Origins of Harmonics on the Power System

Harmonic distortion results from nonlinear loads in the power system. These non linear loads can be grouped into three major categories.

1. Ferromagnetic Devices
2. Electronic Power Converters
3. Arcing Devices

The most common of these on industrial power systems is electronic power conversion equipment. Some examples of this type of equipment are listed below:

- Computer Equipment
- Copy Machines
- Electronic Ballasts
- Facsimile Machines
- Adjustable Speed AC Drives
- Uninterruptable Power Supplies
- DC Drives
- DC Rectifiers

From the IEEE Standard 519, the typical current harmonic spectrum for a three phase 6-pulse converter is shown in the following table.

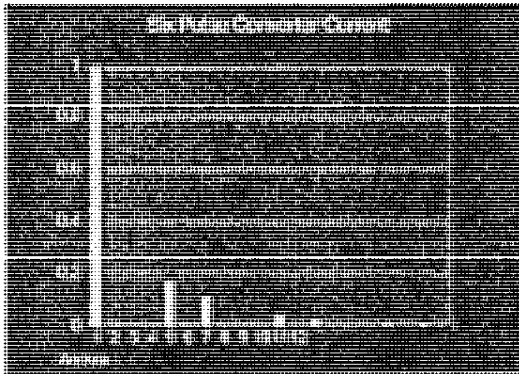


Figure 5

Harmonic	Magnitude
5	17.5%
7	11.1%
11	04.5%
13	02.9%
17	01.5%
19	01.0%

Table 1

Notice that there are no triplen harmonics present in a three phase connection. The typical

current-harmonic spectrum for single phase inverters interfacing a dc source to an ac power system is illustrated below. Triplen harmonics are present for these loads.

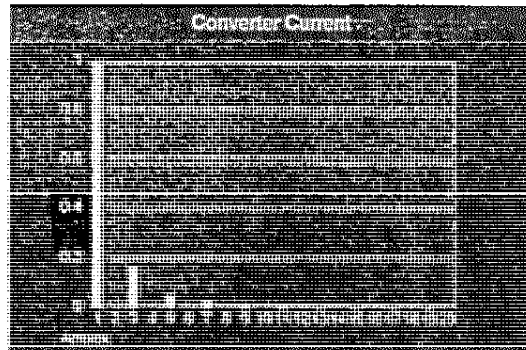


Figure 6

Harmonic	Magnitude
3	16.4%
5	05.2%
7	02.9%
9	02.0%
11	01.5%

Table 2

## Relationship Between Voltage and Current Distortion

Sinusoidal voltage applied to a non linear load yields a distorted current. Likewise, a non sinusoidal voltage applied across a linear load will yield a distorted current. This illustrates a fundamental principle of non linear circuits; either one or both current and voltage may be distorted, however both cannot be sinusoidal.

Power systems are designed to have good voltage regulation at the load. This equates to the source impedance having low impedance compared to the load impedance. Therefore, voltage distortion in most systems is slight (even though it may be above acceptable limits). The following figure illustrates this principle.

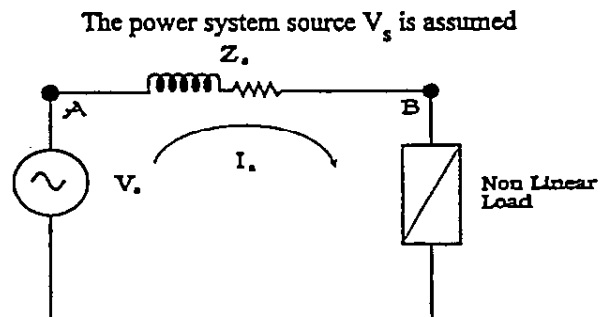


Figure 7

to be an ideal voltage source (Impedance = 0). Therefore there is no voltage distortion at "A". The source supplies power through the distribution network represented by the impedance,  $Z_s$ . The resulting distorted current through this impedance causes the voltage to be distorted at "B". The amount of voltage distortion is dependent upon the value of  $Z_s$  and current magnitude.

The effects of harmonic producing loads are greatly dependent upon the power system characteristics. The presence of harmonic producing loads alone is not a definite indication that there will be an adverse effect to the power system or other connected loads.

## Effects of Current Distortion

Although harmonic currents may not directly affect other power system loads connected to the system if the voltage distortion is low, they may have a severe effect on power delivery elements connecting these loads to the power system. This is especially true for distribution feeders providing power to single phase harmonic producing loads. The following figure illustrates such a system.

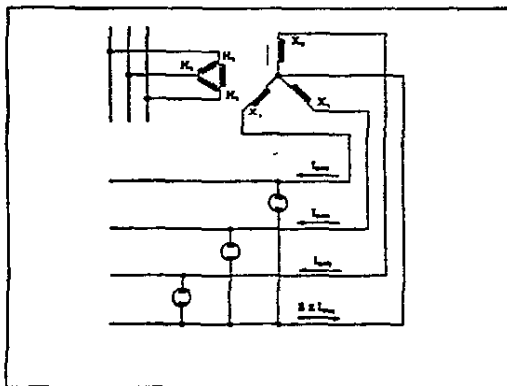


Figure 8

The majority of single phase loads are connected line to neutral. Under conditions where the loads are linear, a balanced three phase load consisting of 60 HZ current, would be delivered by the transformer secondary resulting in insignificant neutral currents. However when these loads are non linear, such as computers or any office equipment which uses a switch mode power supply, the current contains significant amounts of third order harmonic distortion (180 Hz.). These triplen or zero sequence currents add in the neutral. The figure below illustrates this principle. Under balanced conditions, 60 Hz. three phase currents 120° apart equate to zero.

However, 180 Hz currents 120° apart are added together.

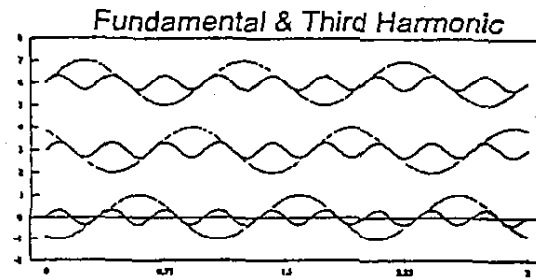


Figure 9

Transformers used in these applications are subjected to severe operating conditions which could result in premature failure. Hysteresis, eddy current, and stray losses in the iron core increase dramatically with harmonic currents present. Additional heating occurs due to the triplen harmonic current becoming trapped within the delta winding. Further the neutral conductor used in these circuits is normally sized equal to phase conductors in order to meet code requirements which would accommodate worst case conditions for linear loads where one phase is fully loaded and the other two unloaded. Also, no overload protection is provided on the neutral conductor since this protection would normally be provided by the protection on the phase conductors. The net result is that the neutral conductor can be significantly overloaded and unprotected leading to catastrophic failure. Other effects of zero sequence harmonics include the following:

- High neutral to ground voltage
- High peak phase current
- High average phase current
- High THD of voltage and current
- Low Power Factor
- Telephone Interference
- Increased apparatus vibration
- *Electronic device malfunction*

## Corrective Solutions

One solution to this problem may be to replace the transformer and neutral conductors with elements which have significantly more capacity and derate them for use on systems with high current distortion. In some cases this may not be economically feasible; in addition fault

current may increase beyond the ratings of the existing protective devices.

Another solution is to remove the harmonic current from the system. This can be achieved by adding a zero sequence filter. Tuned LC filters have been employed to provide this filtering, however for most 208/120 volt applications, the fundamental current is not displaced adequately to allow for the added capacitance on the system. In other words, the added capacitance of a tuned LC filter would create a leading power factor on the system. Perhaps the solution best suited for this application is a zero sequence filter which operates on the principle of an ideal Zig-Zag auto transformer. These filters provide a high impedance to positive and negative sequence currents and an ultra low impedance to zero sequence currents. Caution must be observed when applying these filters. Harmonic current flow, fault levels and single phasing performance must all be evaluated.

## Effects of Voltage Distortion

As described earlier, harmonic voltages are usually caused by the interaction between harmonic currents and the power system impedance. Under normal conditions, this relationship does not result in significant voltage distortion. However, when power factor correction capacitors are applied to a power system where harmonic currents are present, the capacitors and system impedance (inductive) will resonate at a particular frequency. This resonant frequency is dependent upon the amount of capacitance and system inductance. Should this resonant frequency be on or near a harmonic generated by a non linear load, the voltage distortion at that harmonic can be greatly amplified resulting in significant harmonic distortion. This principle is illustrated in the following example.

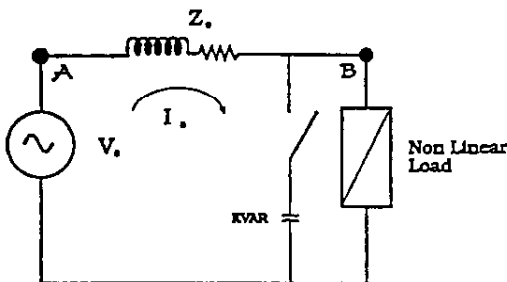


Figure 10

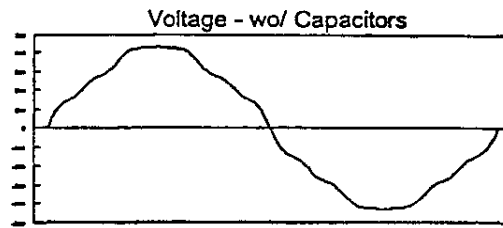


Figure 11

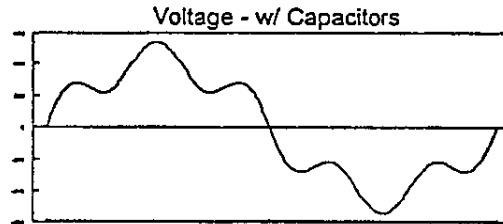


Figure 12

Notice that the system without capacitors results in minimal voltage distortion. However, the same system with the addition of capacitors results in parallel resonance near the fifth harmonic and a significant increase in harmonic distortion is created. Notice the sharp increase in peak voltage.

Harmonic voltage distortion creates harmonic magnetic fluxes within motors. These fluxes contribute little useful work, increase losses, and create excessive heating. The net effect of these harmonics is premature motor failure.

Power Factor Correction Capacitors are the system component most affected by voltage distortion. Thermal failure is caused by excessive RMS current through the capacitors. This is due to the declining impedance value of the capacitor as the frequency increases. Insulation failure is caused by excessive peak voltages. These peak voltages can be as high as the arithmetic sum of the harmonics. Generally, voltage distortion will not be high enough to cause capacitor failures unless the system is resonant at a frequency which there is significant harmonic energy. This is normally the fifth or seventh harmonic..

## Corrective Solutions

Undesirable harmonic voltage distortion can be prevented by altering the flow of harmonic current into the power system. The most common approach is to divert these currents with a low impedance shunt path. This path is provided by a shunt filter. These single tuned filters are an economical and reliable

method for solving harmonic distortion problems.

The application of an LC tuned or "notch" filter is to simply short circuit a particular harmonic current. This filter may also be used to move the resonant frequency of the system safely away from a troublesome harmonic. This is useful in instances when a power system is capable of absorbing the harmonic currents produced by a load except when resonance exists. The fundamental approach to the filter design is;

1. Determine the amount of harmonic current to be filtered and the required harmonic frequency ( $I_{fn}$ ,  $f_n$ ).
2. Select a capacitor size based upon the required harmonic current to be filtered and the 60 Hz reactive power required (MVAR,  $X_c$ ).
3. Determine the reactor impedance needed to achieve the desired tuning ( $X_L$ ).
4. Check the filter response including the effect of component tolerances.
5. Check the peak and steady state voltage across the capacitor including the fundamental and harmonic frequencies ( $V_{peak}$ ,  $V_{rms}$ ).

The following example illustrates this process given the system in figure 10. The existing capacitor bank is used to safely detune the system resonance away from the fifth.

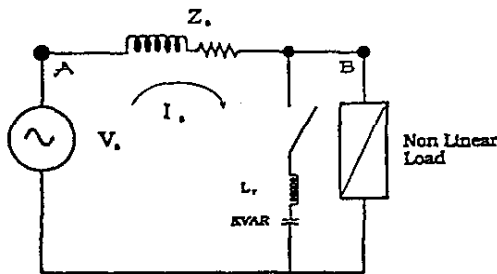


Figure 13

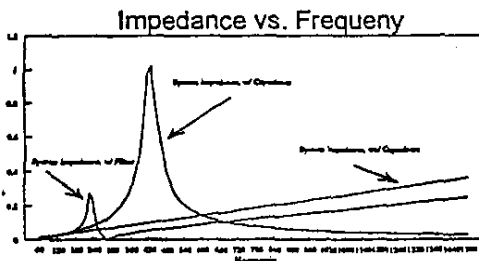


Figure 14

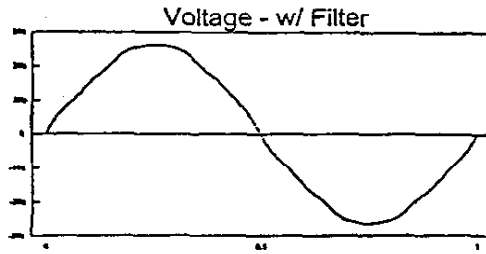


Figure 15

Once the filter components are selected and they are checked to insure that they will operate within their ratings, the expected system results are reviewed.

### Useful Formula

Resonant Frequency

$$f_r = 60 \times \sqrt{\frac{KVA_{ac}}{KVAR_{cap}}}$$

Filter Design Given Capacitor Size & Filter Frequency

Reactor Impedance

$$X_L = \frac{KV^2}{KVAR \times n^2 \times 1000}$$

Filter Duty

$$I_n = \frac{V_{fn}}{X_c - X_L}$$

Total RMS Current (Approximate)

$$I_{rms} = \sqrt{I_n^2 + I_{fn}^2}$$

Fundamental Voltage Across Capacitor

$$V_{c1} = I_n \times X_c$$

Harmonic Voltage Across Capacitor

$$V_{cn} = I_{fn} \times \frac{X_c}{n}$$

Approximate Peak Voltage

$$V_{peak} = V_{c1} + V_{cn}$$

Approximate RMS Voltage

$$V_{rms} = \sqrt{V_{c1}^2 + V_{cn}^2}$$

Approximate Reactive Power of Filter

$$KVAR = 3 \times \sqrt{V_{rms}^2 \times I_{rms}^2}$$